

Bayesian Networks for Estimation of Delay Propagation and Cancellation in the NAS

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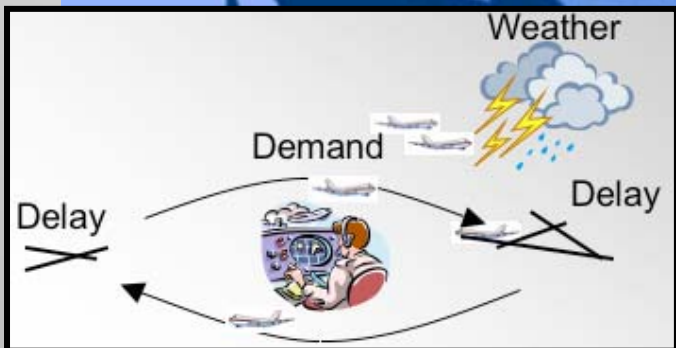
(Joint work with Ning Xu, Kathryn Laskey, George Donohue)



**CENTER FOR AIR TRANSPORTATION
SYSTEMS RESEARCH**



Delay Propagation

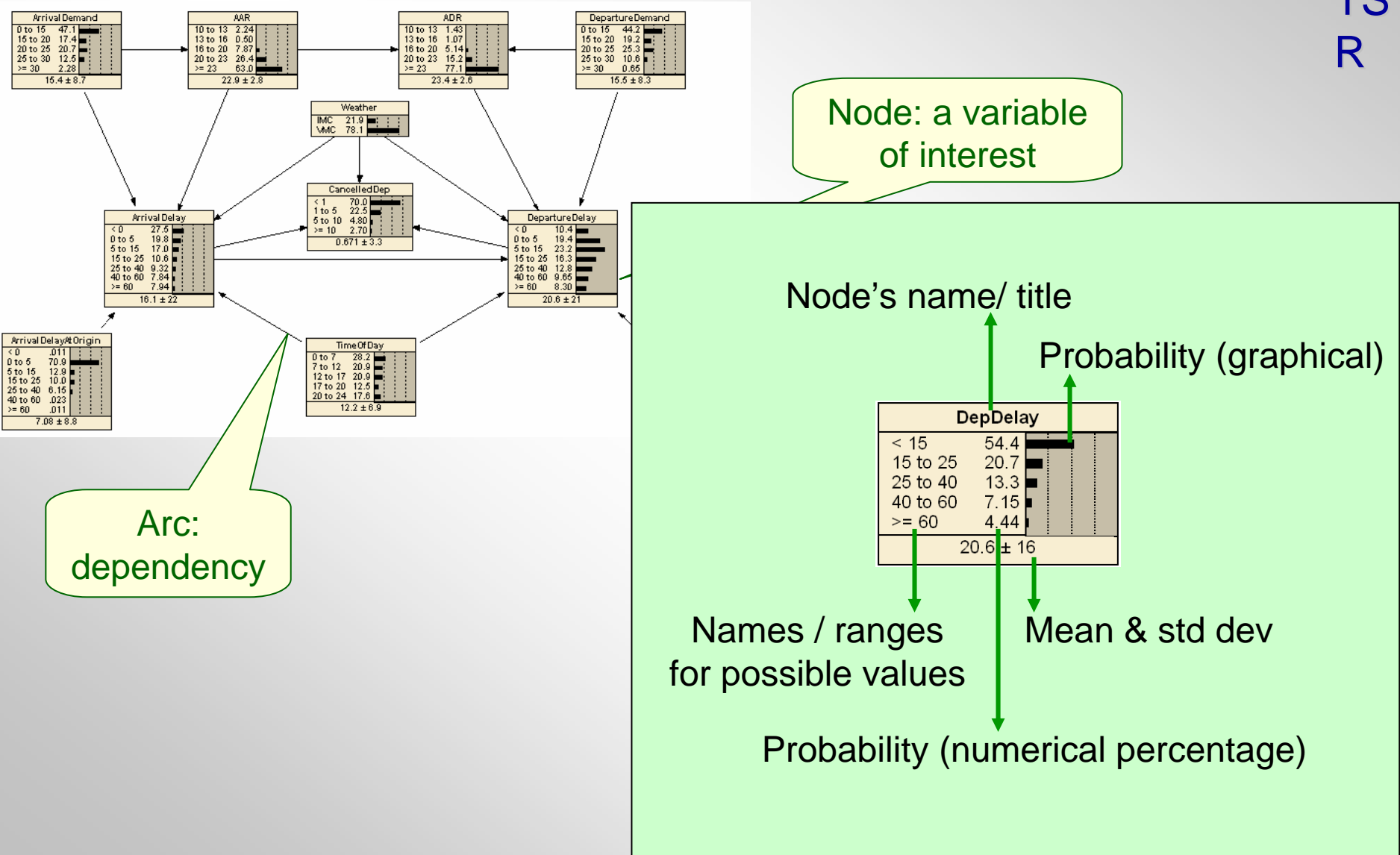




Motivation & Approach

- **Delay/cancellation has steadily increased**
- **Delay at one airport has ripple effect to the whole NAS**
- **Our Bayesian Network can**
 - **Model complex, highly nonlinear, stochastic behaviors for NAS**
 - **Represent interactions between airports**
 - **Capture the complex relationship between variables in NAS, e.g.**
 - **Show how the delays are propagated to different airports under different weather conditions**
 - **Show how cancellation is impacted by other variables**

Notation & Representation



Bayesian Inference

A

DepDelay_ORD	
< 0	6.67
0 to 5	26.1
5 to 15	24.5
15 to 25	18.8
25 to 40	13.8
40 to 60	7.32
>= 60	2.84

$P(A)$: the probability of A (prior)

$$P(a_i < A < a_j) = F(a_j) - F(a_i) = \int_{a_i}^{a_j} f(x) dx$$

B

DepDelay_ORDtoDFW	
< 0	6.16
0 to 5	76.8
5 to 15	6.56
15 to 25	3.69
25 to 40	3.13
40 to 60	1.91
>= 60	1.77

$P(B)$: the marginal probability of B

$$P(B) = P(b_i < B < b_j) = \int_{b_i}^{b_j} \int_{-\infty}^{\infty} g(y, x) dx dy$$

C

ArrDelay_DFW_ORD(+2:15)	
< 0	20.6
0 to 5	55.7
5 to 15	8.38
15 to 25	4.70
25 to 40	4.02
40 to 60	3.05
>= 60	3.49

$$P(B) = \sum_i P(B|A_i)P(A_i)$$

$P(A|B_j)$: the posterior probability of A given B_j

$$P(A|B_j) = \frac{P(B_j|A)P(A)}{P(B_j)} \quad \text{[Bayes Rule]}$$

DepDelay_ORD	
< 0	0.89
0 to 5	0.69
5 to 15	3.17
15 to 25	11.5
25 to 40	29.8
40 to 60	29.2
>= 60	24.7

DepDelay_ORDtoDFW	
< 0	0
0 to 5	0
5 to 15	0
15 to 25	0
25 to 40	0
40 to 60	100
>= 60	0

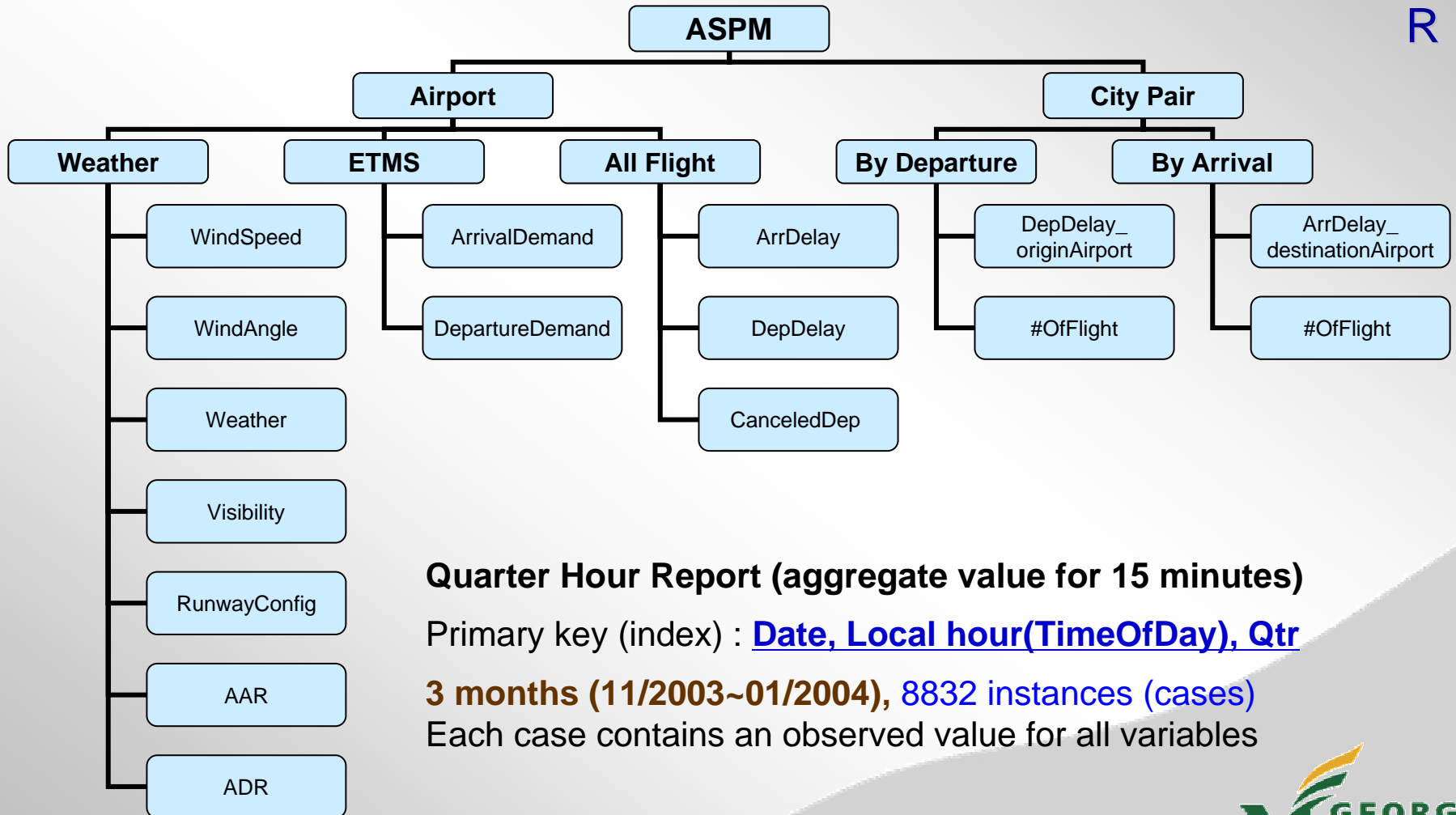
ArrDelay_DFW_ORD(+2:15)	
< 0	1.22
0 to 5	2.44
5 to 15	5.49
15 to 25	17.7
25 to 40	30.5
40 to 60	23
>= 60	13.4

$P(C|B_i)$: the conditional probability of C given B_i
(likelihood)

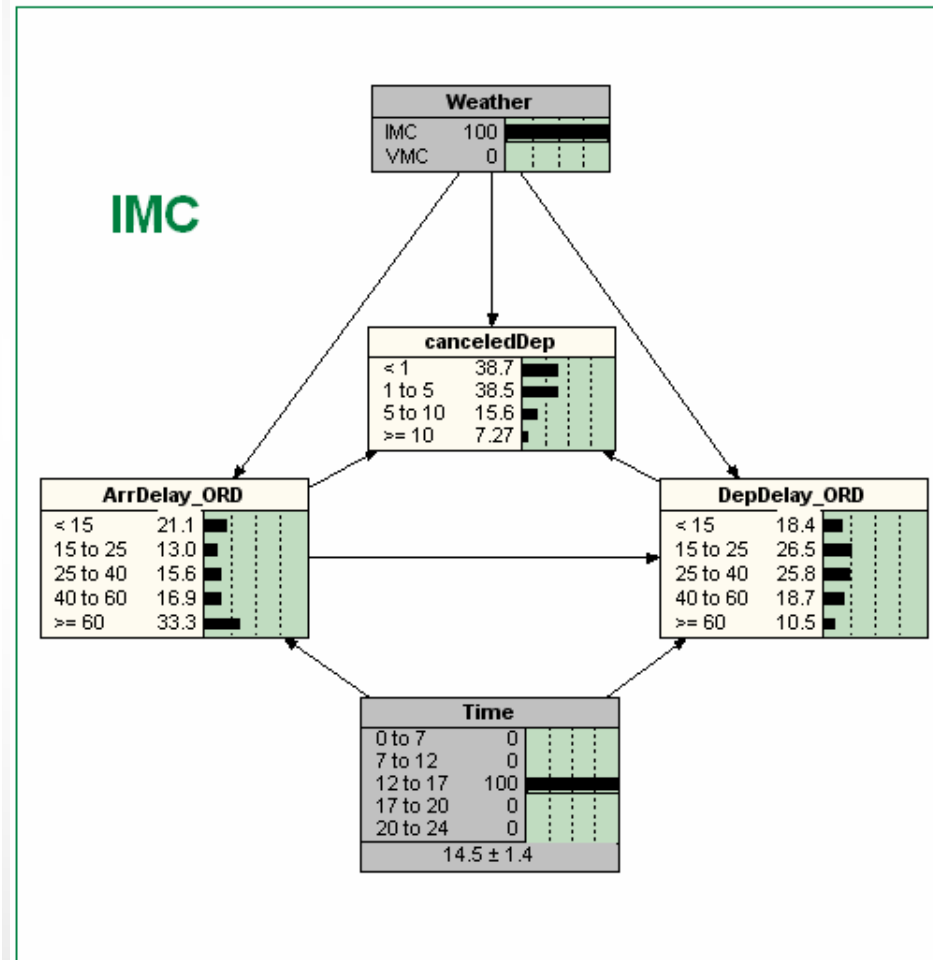
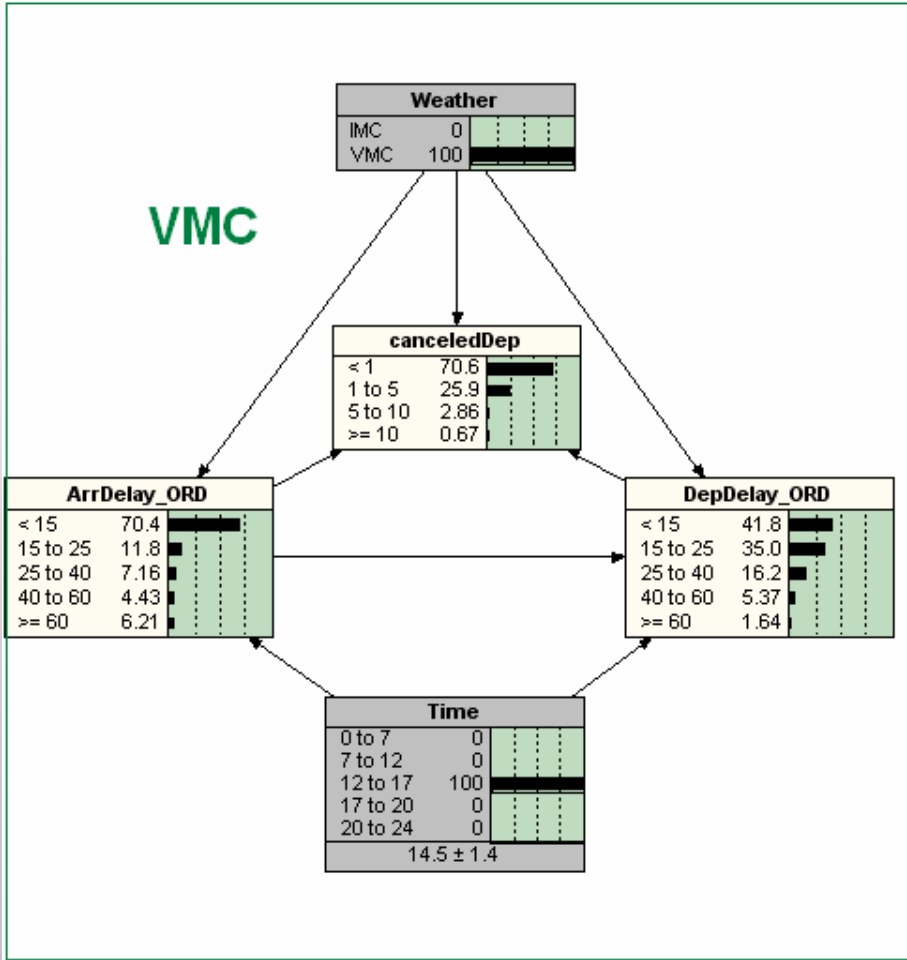
Delay Propagation



Data for Constructing Model



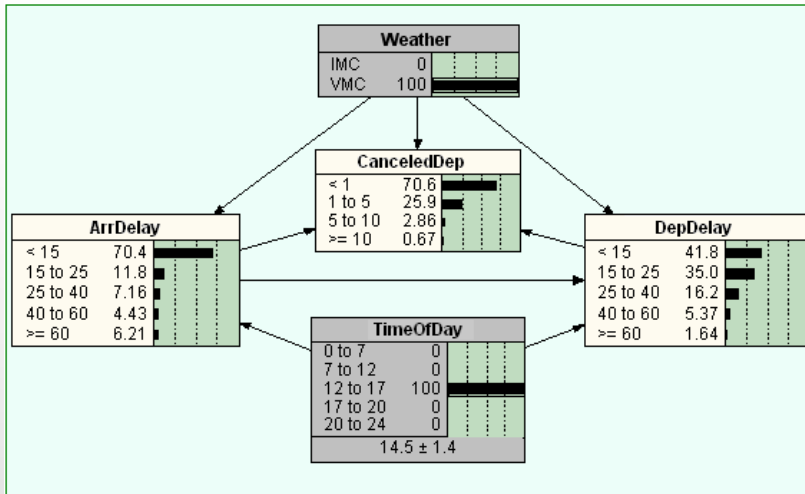
ORD: Delay & Cancellation



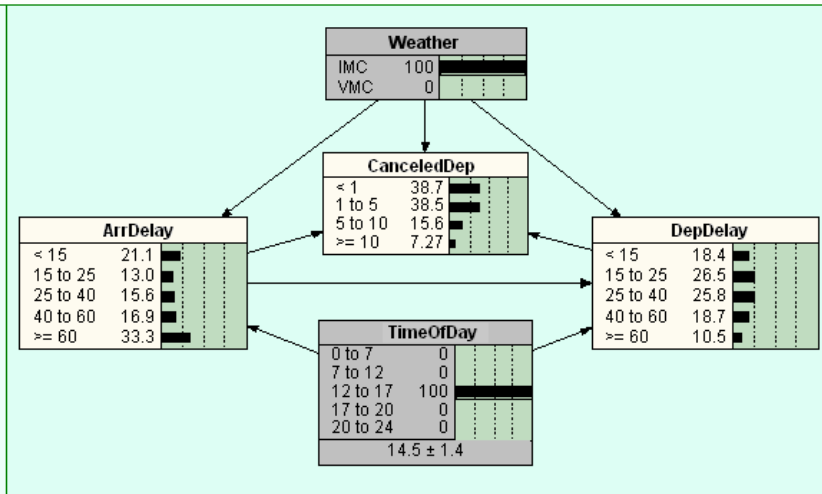
Example: Comparing Airports

ORD

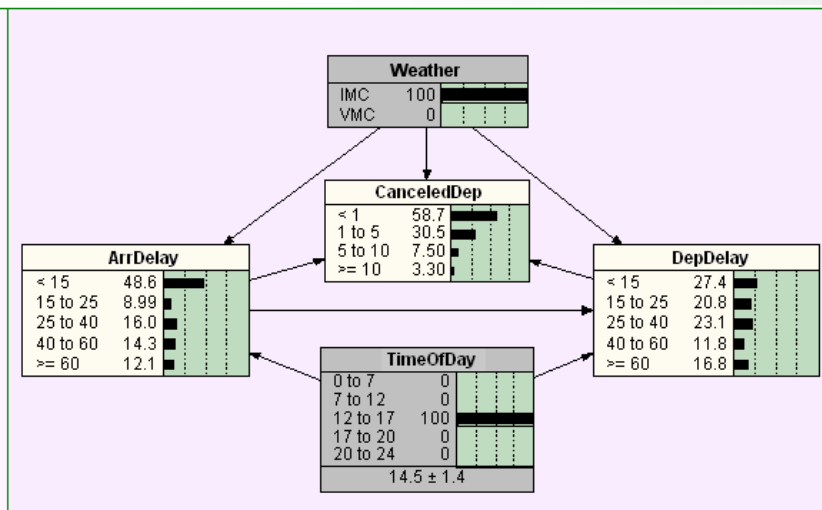
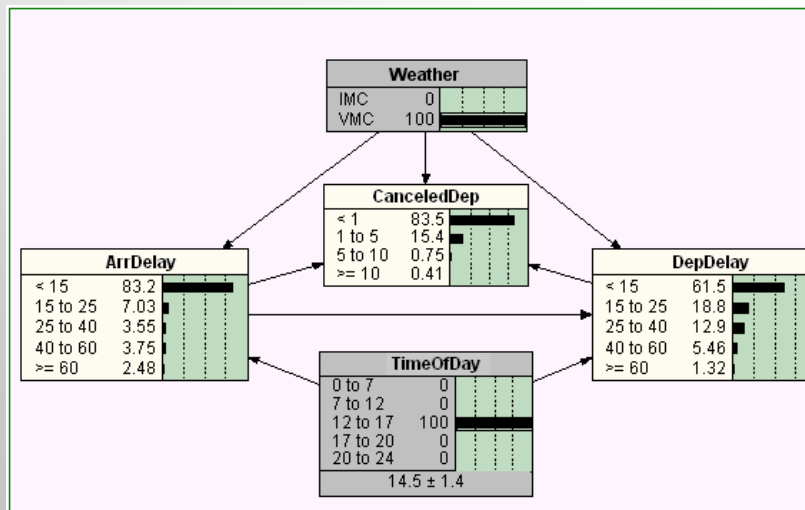
VMC



IMC

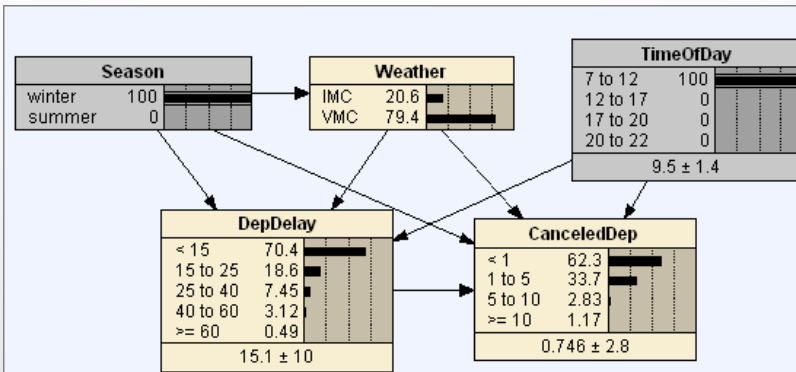


LGA

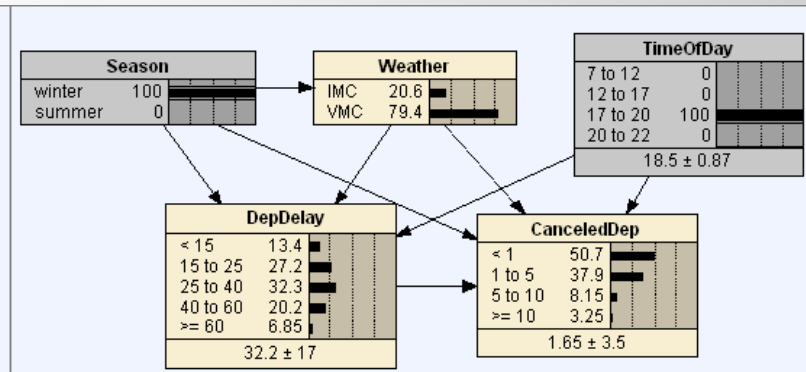


Flight Cancellation (ORD)

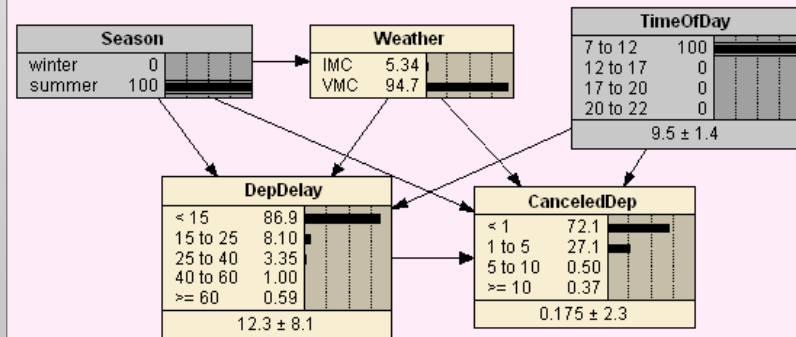
Winter vs. Summer; Morning vs. Evening



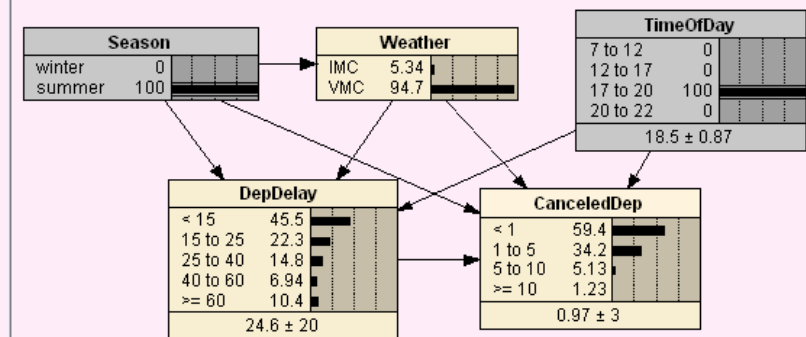
Winter Morning



Winter Evening

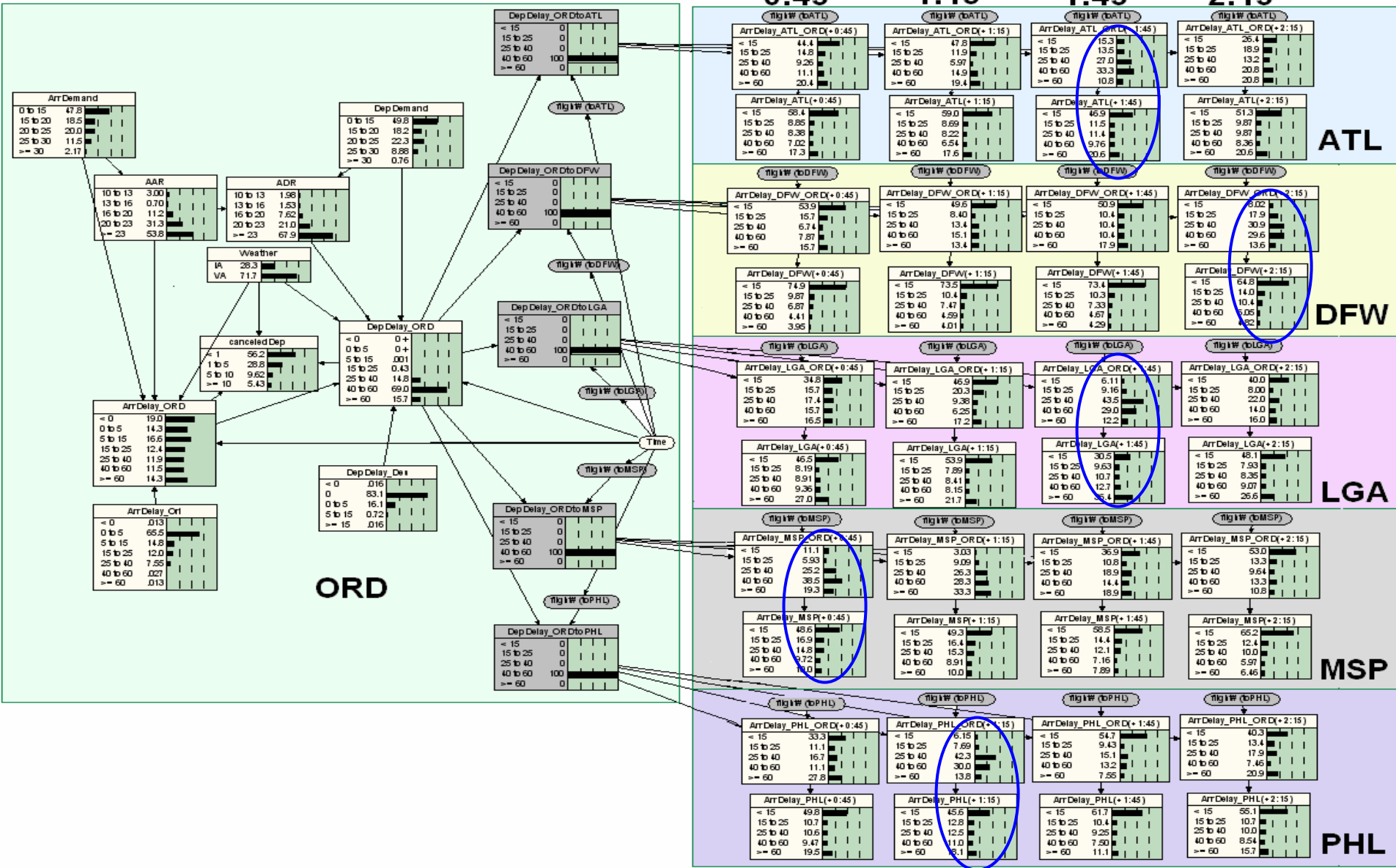


Summer Morning



Summer Evening

Delay Propagation from ORD

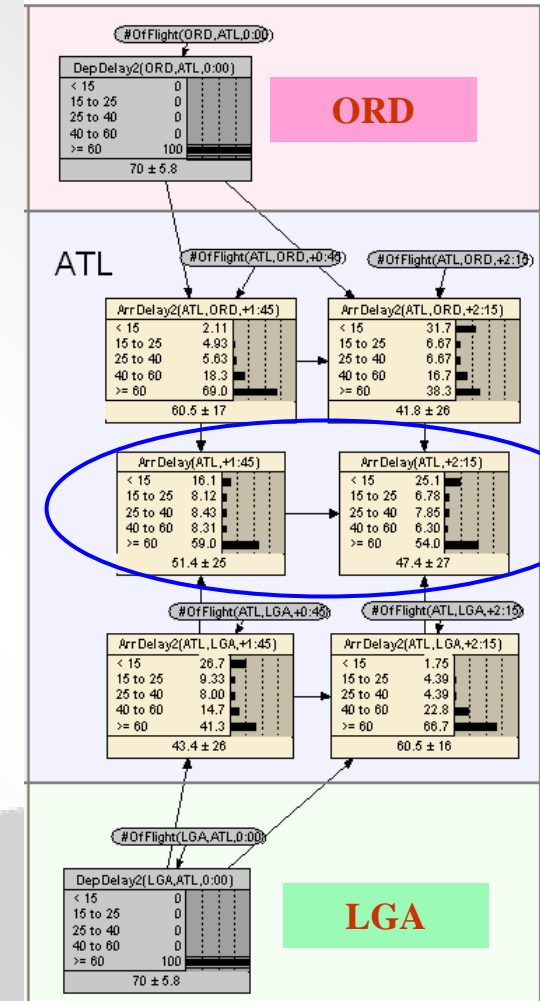
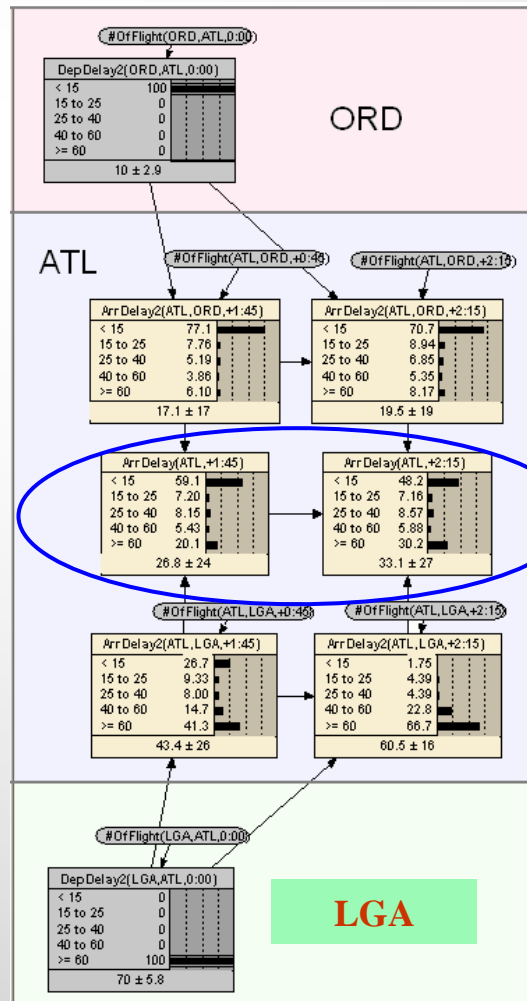
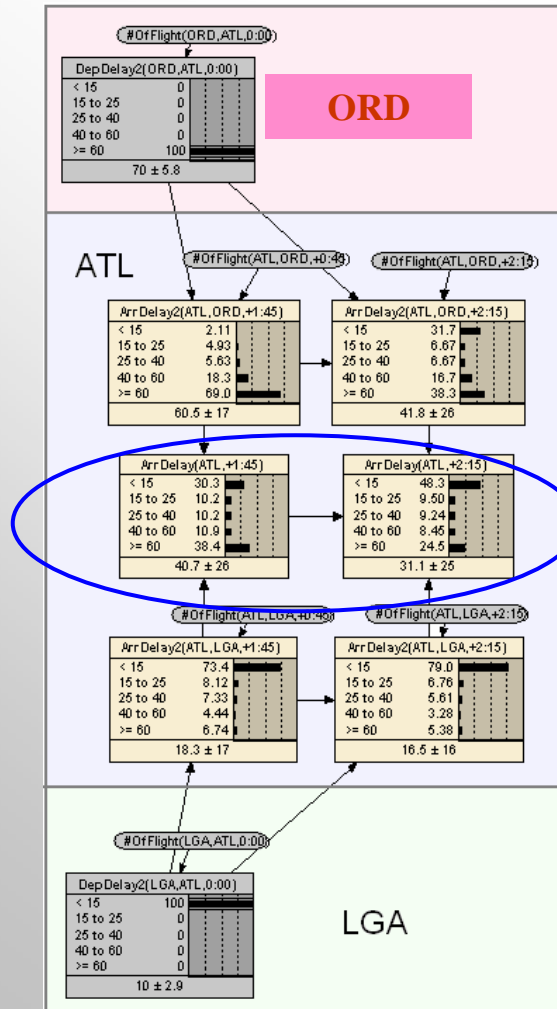


Delay Propagation Into ATL

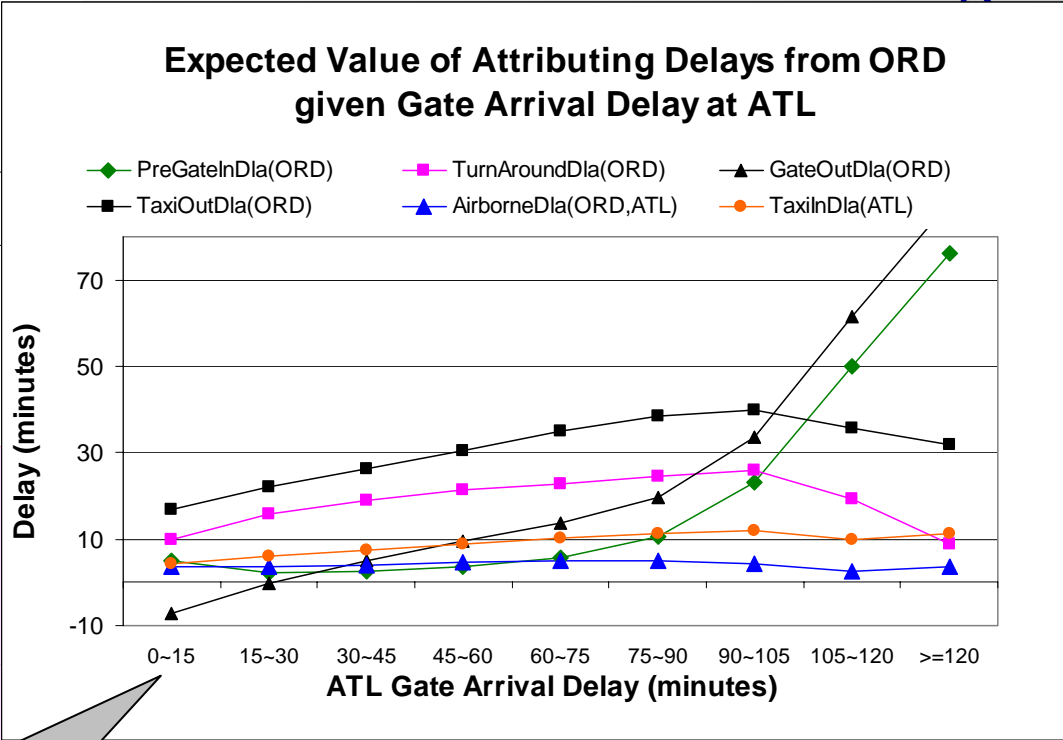
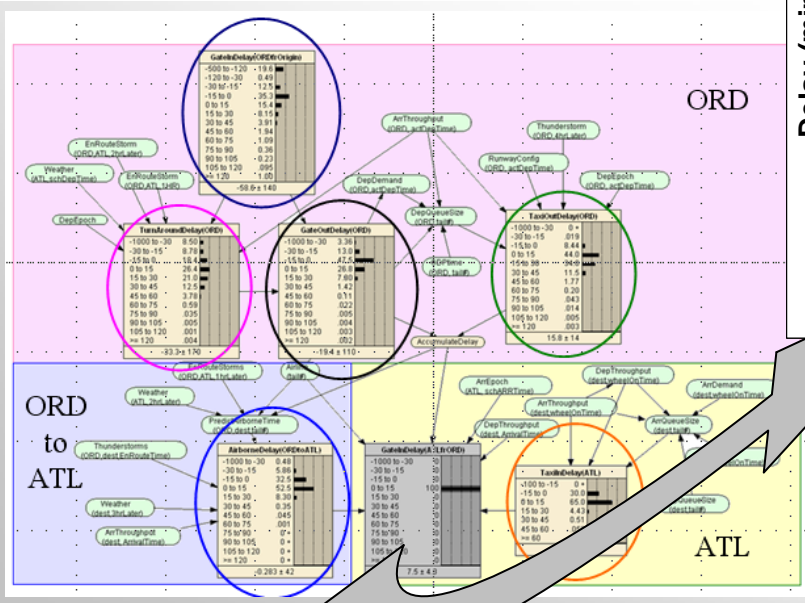
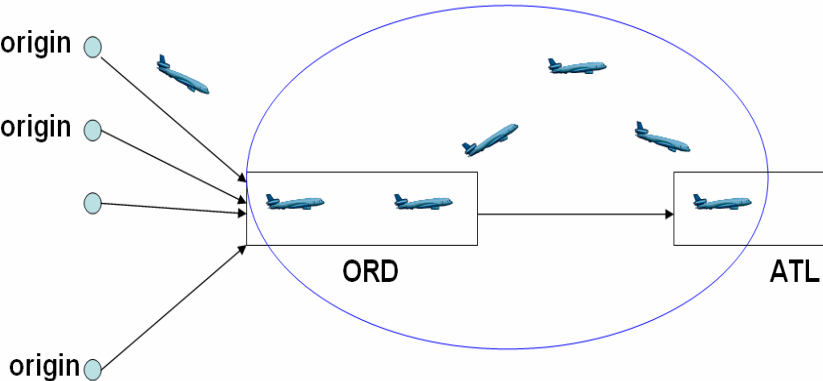
Scenario 1 - ORD Delay

Scenario 2 - LGA Delay

Scenario 3 - Both Delay

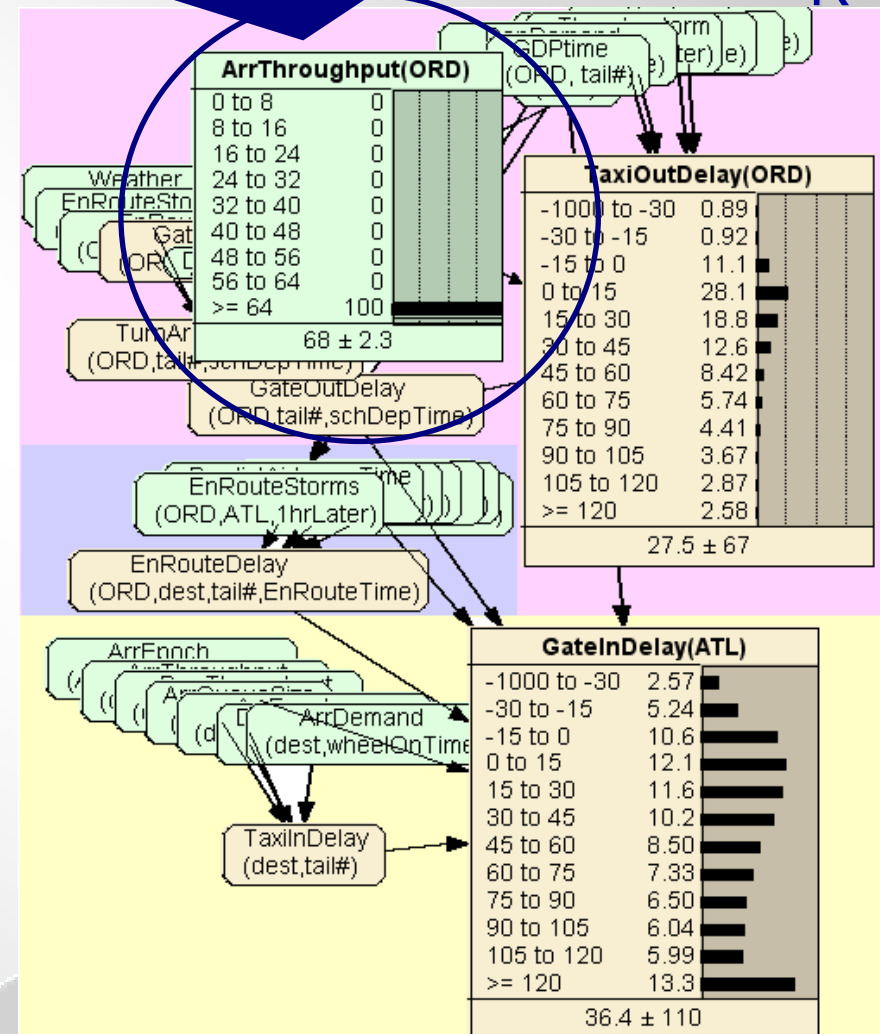
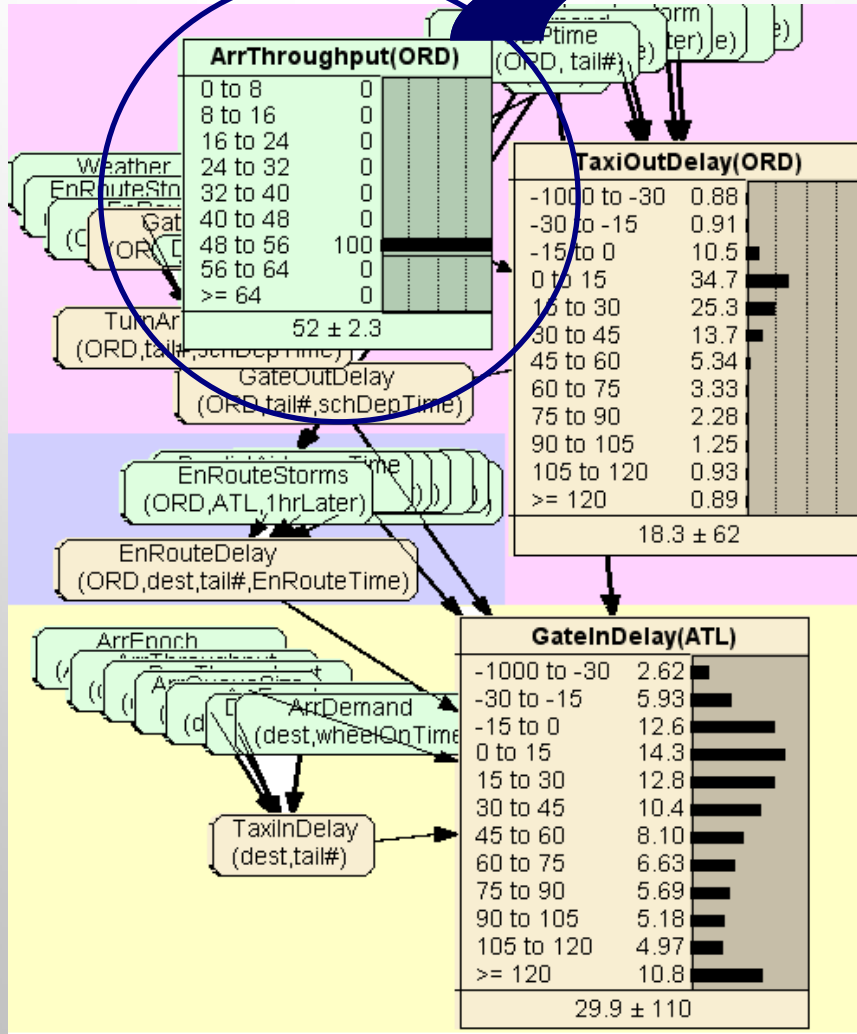


Decomposing Delay



Given evidence for GateInDelay(ATL,ORD)

What If Scenarios



Conclusions



- **Constructed stochastic model to represent relationship for variables in NAS**
- **Applied model to analyze cause & effect**
 - **Impact of weather on delay & cancellation**
 - **Effects of season and time of day**
 - **Propagation of delay from airport to airport**
 - **Major contributing factors to each phase of delay**
- **Model is complementary with simulation models**

Acknowledgements

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Thank You



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