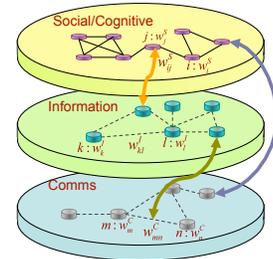


Network Science

- A network is a collection of nodes, agents, ...
 - that collaborate to accomplish actions, gains, ...
 - that cannot be accomplished without such collaboration
- Network science
 - The Internet and other communication networks
 - Social networks
 - Biological networks
- Fundamental knowledge is necessary to design large, complex networks in such a way that their behaviors can be predicted prior to building them. (From National Research Council report on Network Science -- The National Academies Press, 2005)

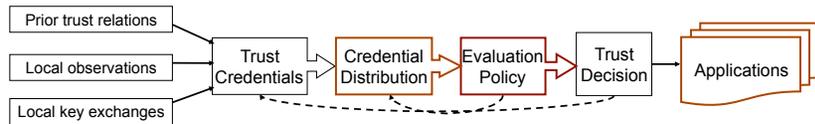
Case study: Trust Management

- Multiple Interacting Graphs (Directed graphs)
 - Nodes**: agents, individuals, groups, organizations
 - Links**: ties, relationships
 - Weights on links**: value (strength, significance) of tie
 - Weights on nodes**: importance of node (agent)
- Value directed graphs with weighted nodes
- Real-life problems: **Dynamic, time varying graphs, relations, weights**



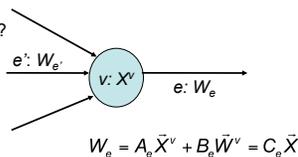
Organizational needs
Network architecture and operation

- Objective: use mathematical analysis to understand and predict the emergent behaviors of distributed trust management systems in autonomic networks.



Trust Credential Distribution

- No centralized trusted party; trust credentials are scattered in the network.
 - Where and how to find all needed credentials?
 - Where and how to store credentials such that searching is efficient?
- Network Coding Based Scheme**
 - Extremely simple to implement
 - Only local information exchange
 - Easy for discovering new credentials
 - Efficient distribution



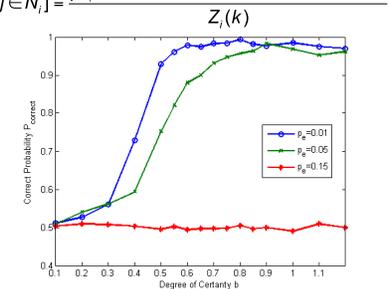
Trust Evaluation Policy

- The trustworthiness of an agent is based on other peers' opinion
 - The most straightforward scheme is to ask neighbors to "vote" for it.
- Iterated stochastic voting**: $\Pr[s_i(k+1) | s_j(k), j \in \hat{N}_i] = \prod_{j \in \hat{N}_i} \Pr[d_{ij}, d_{ji} | s_j(k+1), s_j(k)] + \Pr[s_i(k+1)]$
- Convergence**: unique stationary distribution.

Phase transitions in two parameters:

- Degree of certainty b
- Probability of error p_e

Theoretical analysis: results in the Ising model and the spin glass model, where $d_{ij} = J_{ij}$; replica method.



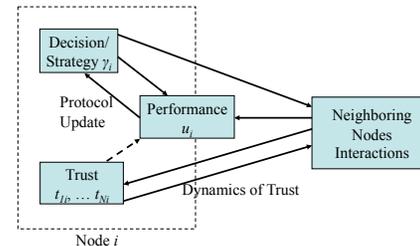
Case study: Collaboration

- The nodes gain from collaborating
- But collaboration has costs (e.g. communications)
- Fundamental trade-off**: gain from collaboration vs cost of collaboration

Constraint Coalitional Game

- Network formation game**:
 - Payoff of node i from the network G is defined as $v_i(G) = \text{gain} - \text{cost}$
 - Iterated process
 - Node pair ij is selected with probability p_{ij}
 - If link ij is already in the network, the decision is whether to sever it, and otherwise the decision is whether to activate the link

Trust and Collaboration



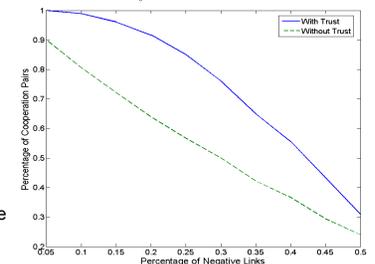
Two linked dynamics:

Trust propagation and game evolution

$$\gamma_i(k+1) = f^i(u_i(k), \gamma_i(k), \gamma_j(k), t_{ji}(k))$$

$$t_{ij}(k) = g^i(\gamma_j(k), t_{ij}(k-1), t_{ij}(k), v_{ji}^i(k)), \forall h \in N$$

$$u_i(k) = h^i(\gamma_i(k), \gamma_j(k))$$



Objective:

- to find what form or policy can induce all (or most) nodes to collaborate: **maximize** the coalition.

Two solutions:

- Negotiation**: Players with positive gain can negotiate with their neighbors by sacrificing certain gain.
- Trust**: By introducing a trust mechanism, all nodes are induced to collaborate without any negotiation.